

GUJARAT TECHNOLOGICAL UNIVERSITY**B. Pharm. - SEMESTER– I, EXAMINATION – SUMMER-2016****Subject Code: 210006****Date: 07/06/2016****Subject Name: Elementary (Remedial) Mathematics****Time: 02:30 PM to 05:30 PM****Total Marks: 80****Instructions:**

1. Attempt any five questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.

Q.1 (a) Solve the following equations. **06**

1) $2x(x - 7) = 3(2 - x)$

2) $5x^2 - 2x - 4 = 0$

(b) Prove the following trigonometric identity **05**

$$(1 + \cot \theta)^2 + (1 - \cot \theta)^2 = 2 \operatorname{cosec}^2 \theta$$

(c) Find $\frac{dy}{dx}$, if $x = a(\theta + \sin \theta)$, $y = a(1 - \cos \theta)$ **05**

Q.2 (a) A card is drawn at random from a pack of 52 cards. What is the probability that the card is a spade or a king? **06**

(b) There are two boxes A and B containing 4 Aspirin, 3 Analgin and 3 Aspirin, 7 Analgin. A box is chosen at random and a tablet is drawn from it. If the tablet is an Aspirin, find the probability that it is from box A. **05**

(c) Calculate the mean and standard deviation for the following table giving the age distribution of 542 members. **05**

Age in years	20-30	30-40	40-50	50-60	60-70	70-80	80-90
No. Of members	3	61	132	153	140	51	2

Q.3 (a) i) Show that the points (1, 1), (-2, 7) and (3, -3) are collinear. **06**

ii) If the distance between A(5, a) and B(2, 6) is $3\sqrt{2}$, find the value of a.

(b) Find the equation of locus of a point which moves such that it remains equidistance from the points A(3, -1) and B(4, 2). **05**

(c) Find the equation of the perpendicular bisector of the line segmnt joining the points A(2, 3) and B(6, -5). **05**

Q.4 (a) Find the value of following i) ${}_{11}P_3$ ii) ${}_6P_2 \times {}_7P_2$. **06**

(b) Find m and n if $(m + n) P_2 = 56$ and $(m-n) P_2 = 12$. **05**

(c) In how many ways can the letters of REARRANGE be permuted? **05**

- Q.5** (a) A club has 14 male and 16 female members. A committee Composed of three women is formed. In how many ways can this be done? **06**
- (b) Evaluate $\lim_{x \rightarrow 2} \frac{4(x^2 - 4)}{x - 2}$. **05**
- (c) Find the value of $(19)^4$ and $(999)^4$. **05**
- Q.6** (a) Integrate the following functions with respect to x **06**
- i) $2x - 3 \cos x + e^x$ ii) $\frac{\cos x}{\cos x - 1}$
- (b) Evaluate $\int \frac{2x+1}{\sqrt{x^2 - 2x+5}}$. **05**
- (c) Evaluate $\int_0^{\frac{\pi}{2}} \log \sin x \, dx$. **05**
- Q.7** (a) Solve the following simultaneous equations using Cramer's rule. **06**
- $$x + y + z = 4$$
- $$2x - 3y + 4z = 33$$
- $$3x - 2y - 2z = 2$$
- (b) A population grows at the rate of 8% per year. How long does it take for the population to double? **05**
- (c) Find the tenth term of a geometric progression whose third term is 16 and whose seventh term is 1. **05**
