

**GUJARAT TECHNOLOGICAL UNIVERSITY****ME – SEMESTER IV (NEW) – • EXAMINATION – SUMMER 2016****Subject Code: 2744101****Date:04/05/2016****Subject Name: Advanced Topics in Signal and Image Processing****Time:10:30 am to 01:00 pm****Total Marks: 70****Instructions:**

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.

- Q.1 (a)** Obtain the Direct Form I and II realizations for a third-order IIR Transfer function which is expressed as below: **07**

$$H(z) = \frac{0.28 Z^2 + 0.319Z + 0.04}{0.5Z^3 + 0.3Z^2 + 0.17Z - 0.2}$$

- (b)** Explain: Poly-phase Realization of FIR Filters. **07**

Draw the Poly-phase realization of the system transfer function,

$$H(z) = 1 - 4Z^{-1} - 3Z^{-2} + 6Z^{-3} - 9Z^{-4} + 5Z^{-5} + 7Z^{-6}$$

- Q.2 (a)** Do the following: **07**

- (1) Prove that filter with the following response has linear phase response:

$$h(n) = \{2,1,1,2\}$$

- (2) An FIR filter (M=11) is characterized by the following transfer function,  $H(z) = \sum_{n=0}^{M-1} h(n)z^{-n}$ . Determine the magnitude response and also prove that the phase and group delay are constant.

- (b)** Design a Low Pass FIR filter using frequency sampling technique having cutoff frequency of  $\frac{\pi}{2}$  rad/sample . The filter have linear phase 4 and length 17. The **07**

$$\text{Desired filter response is } H_d(\omega) = \begin{cases} e^{-j\omega(\frac{M-1}{2})}, & \text{for } |\omega| \leq \omega_c \\ 0, & \text{elsewhere} \end{cases}$$

**OR**

- (b)** Compare the followings: **07**

- (1) Window design method and Frequency sampling method.
- (2) Impulse Invariant and Bilinear Transformation method.

- Q.3 (a)** Design a single pole low pass digital filter with 3dB bandwidth of  $0.2\pi$  by use of bilinear transformation applied to analog filter,  $H_a(s) = \frac{\Omega_c}{s + \Omega_c}$ , where  $\Omega_c$  is the 3dB bandwidth of analog filter. **07**

- (b)** Explain Elliptic Filters in details with suitable mathematical equations. **07**

**OR**

- Q.3 (a)** Determine  $H(z)$  using Impulse Invariant method at 5Hz. Sampling frequency from  $H_a(s)$  as given below: **07**

$$H_a(s) = \frac{2}{(s+1)(s+2)}$$

- (b)** Explain Butterworth filter approximation method in detail with suitable mathematical equations. **07**

- Q.4 (a)** Explain: Up-Sampler in detail with suitable equations. **07**

